

How to graph a SYSTEM OF INEQUALITIES

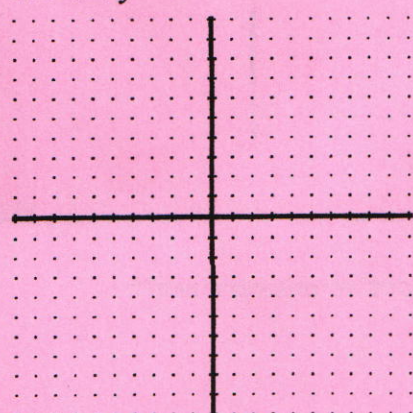
A System of Inequalities is a problem that looks like this:

$$x + y \leq 8, \text{ and } y \geq 3 \text{ and } x \geq 2$$

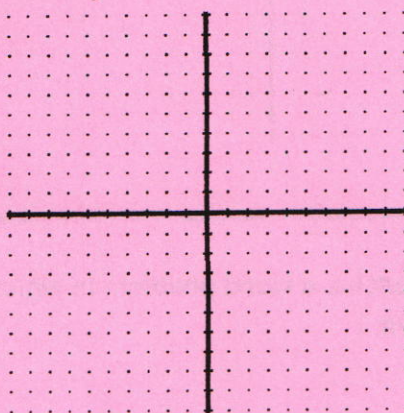
To graph a system like this we are going to graph the three inequalities separately.

Graph each of the following:

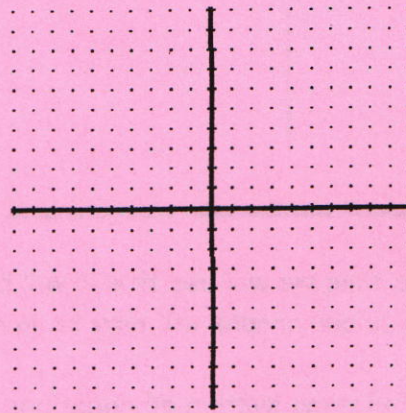
#1 $x + y < 8$



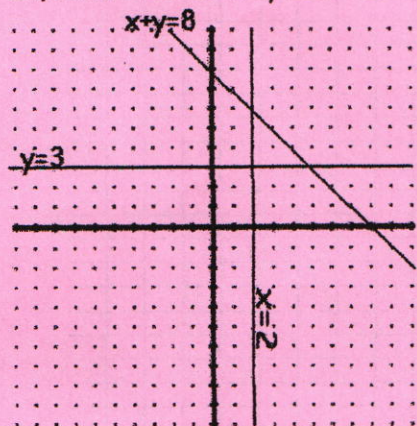
#2 $y \geq 3$



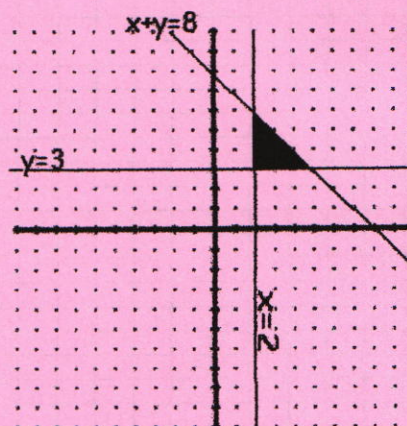
#3 $x \geq 2$



But, since this is a system of equations, we want to put all of these equations on a single graph:

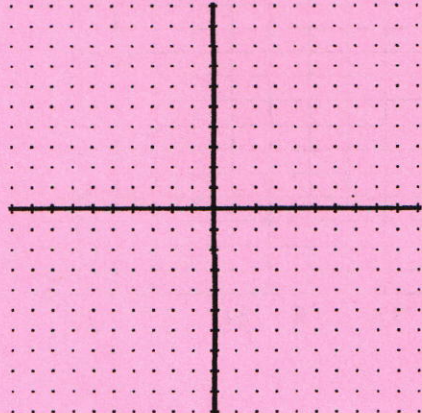


Then, we want to shade only the part of the graph that is shaded by all 3 graphs

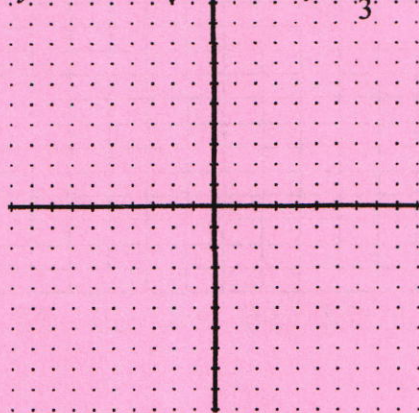


Graph each of the following systems of inequalities in the graph given.

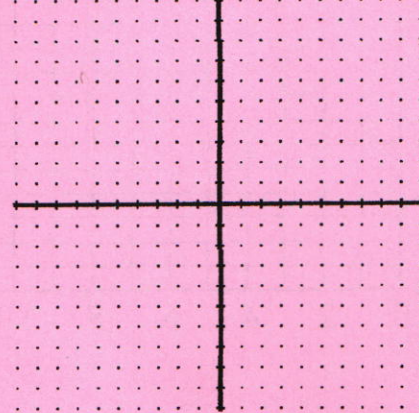
4. $x > 2$ $x < 7$



5. $y \geq -3$ $y \leq 4$ $y \geq \frac{1}{3}x - 1$



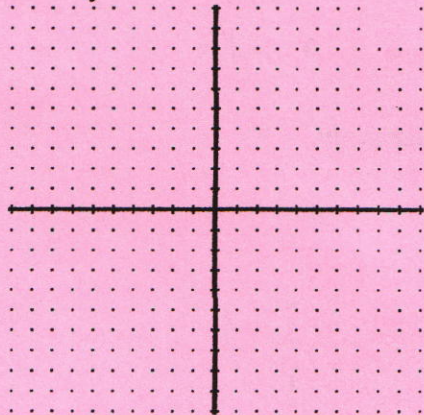
6. $x \leq 5$ $y \geq 3x - 4$



Graph each of the following systems of equations:

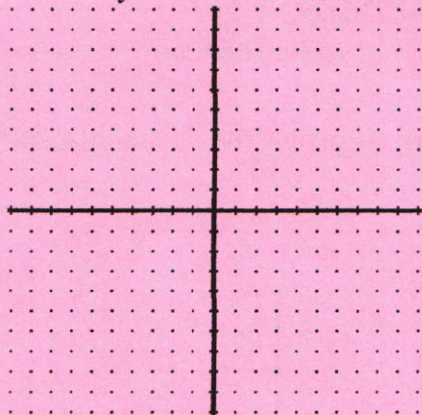
7. $4 \geq y \geq 2$

$2x + 3y \geq 12$



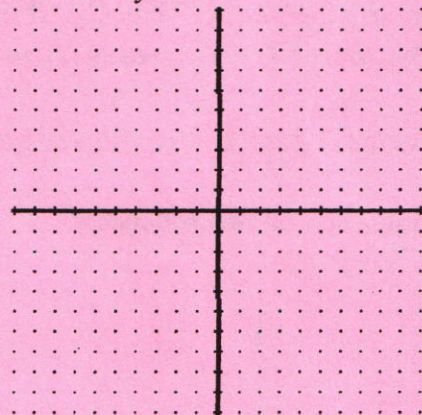
8. $-3 < y < -1$

$y \geq x - 4$



9. $6 \geq x \geq 4$

$3 \geq y \geq -6$



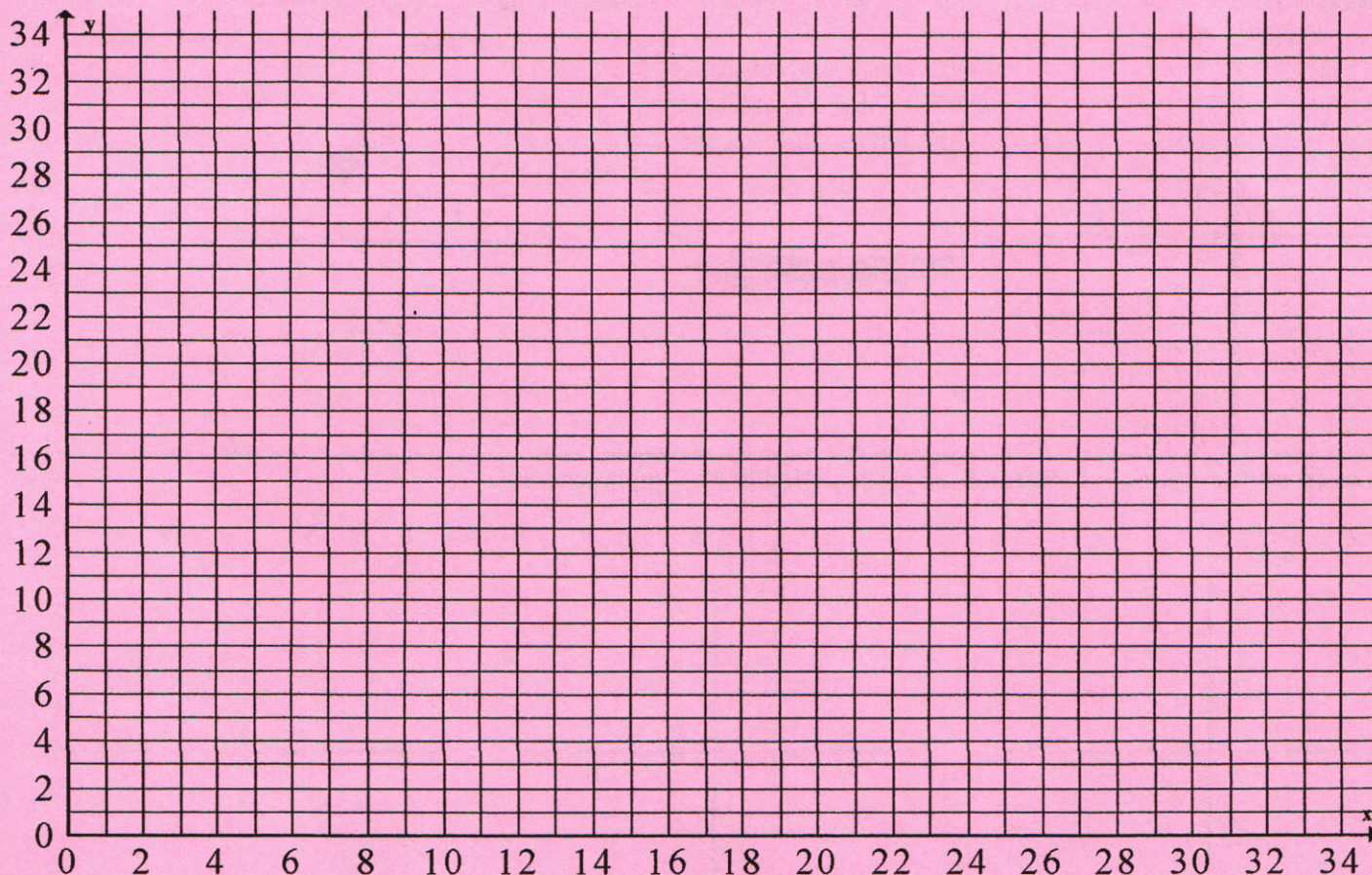
Most of the time we will use this it will be to resolve a word problem in which negative answers won't make sense so our graphs will only be in quadrant 1

Graph the following system of equations:

$x + y \leq 30$

$x \leq 12$

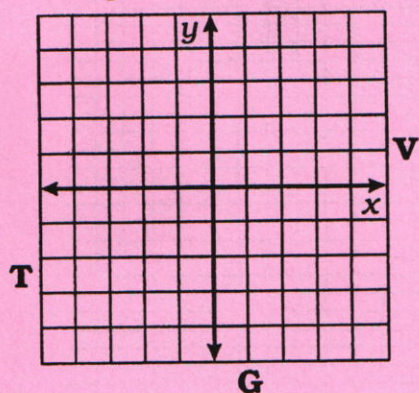
$6x + 10y \geq 90$



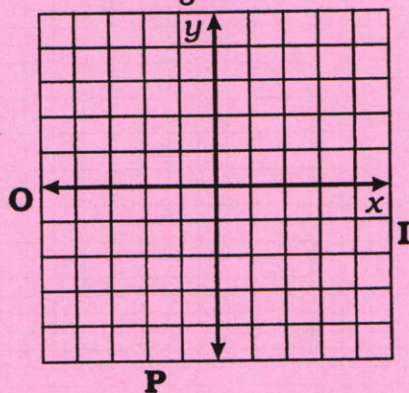
Which Member of Fred Ferd's Family Thinks He's a Pen?

Show the solution region for each system with crosshatching or shading. The crosshatching or shading, if extended, would cover a letter. Write this letter in each box with the exercise number.

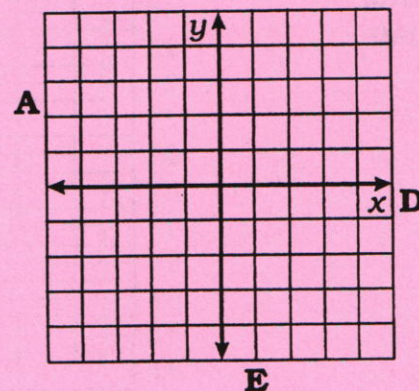
1. $y \geq \frac{3}{4}x - 2$
 $y \leq 1$



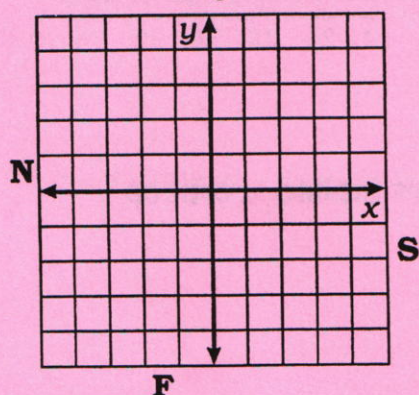
2. $y \geq -2x - 3$
 $y \leq \frac{1}{3}x + 2$



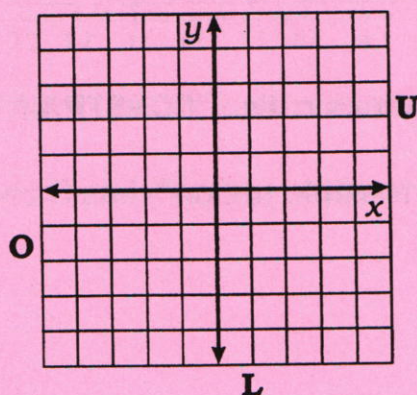
3. $y < \frac{3}{2}x + 3$
 $y < -x + 1$



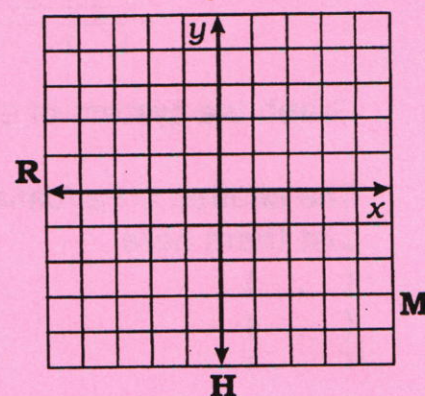
4. $y \leq x$
 $5x + 3y > -6$



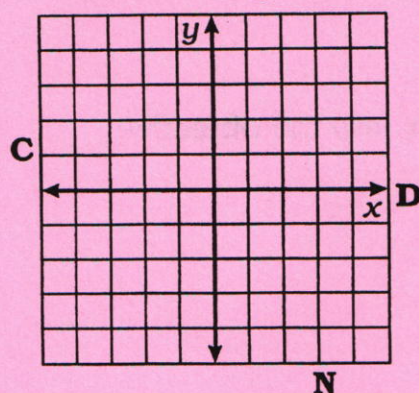
5. $y + 3 > 0$
 $-2x - 5y \geq 5$



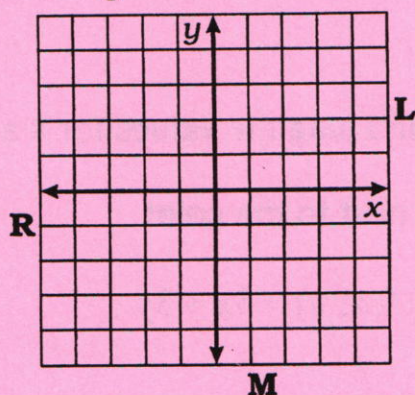
6. $x < 2$
 $x - 2y > 6$



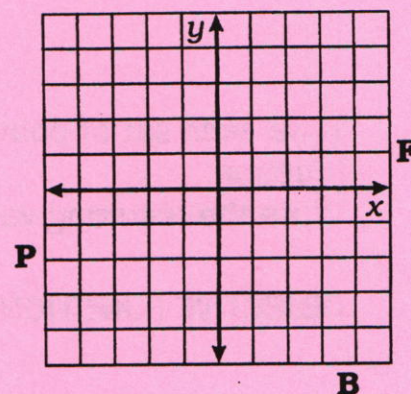
7. $8x + 12y < 24$
 $35x - 20y \leq 80$



8. $10x + 10y \leq 30$
 $y - 3x > 0$



9. $y + 2 \leq 0$
 $2 - x \leq 0$



6

2

4

9

2

7

9

8

5

1

6

3

8

Graphing Systems Of Inequalities Pt. 2
LINEAR PROGRAMING

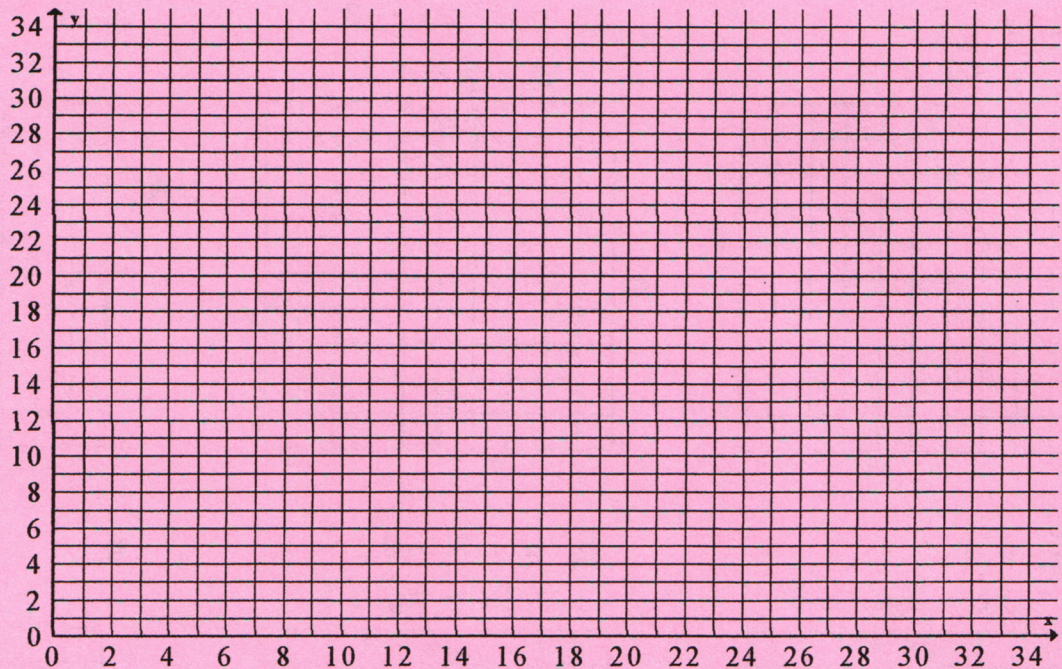
Linear Programming: is full of strange steps:

Constraints:

$$4x + 5y \leq 100$$

$$y \leq x + 11$$

$$x \leq 10$$



Step 1: Graph the system of equations called "CONSTRAINTS"

Step 2: The shaded area (called "feasible region") has 5 corners (called "vertices")
List them here

(,)

(,)

(,)

(0, 0)

(,)

Step 3: Take each set of points and plug the values for X and Y into the objective function.

Write the resulting value next to the point

OBJECTIVE FUNCTION: $f(x, y) = 5x + 3y$

Step 4: Which point gives the highest value in the objective function? _____

Which point gives the lowest value in the objective function? _____

1. Graph and shade the constraints (restrictions).
2. Find the vertices of the shaded region (feasible region).
3. Evaluate each vertex in the objective function.
4. Identify which vertex provides the maximum value and minimum value in the objective function.

Objective Function:

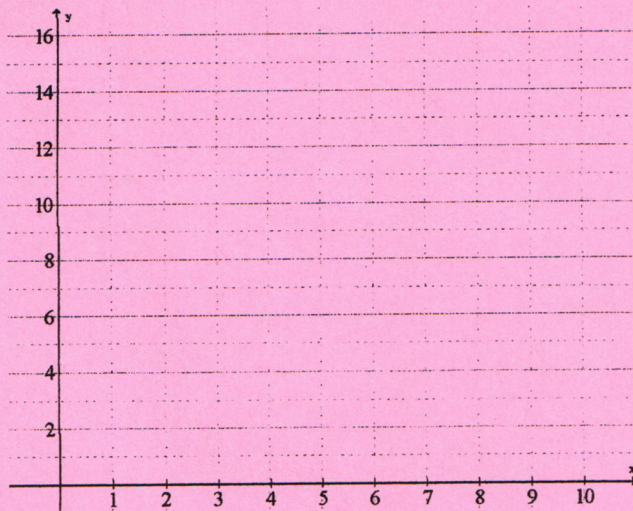
$$2x + 5y =$$

Constraints:

$$y \leq 13$$

$$x \leq 9$$

$$y \geq x$$



Vertices: (,) →

(,) →

(,) →

(,) →

Which vertex gives the max value?Which vertex gives the min value?

Objective Function:

$$5x - y =$$

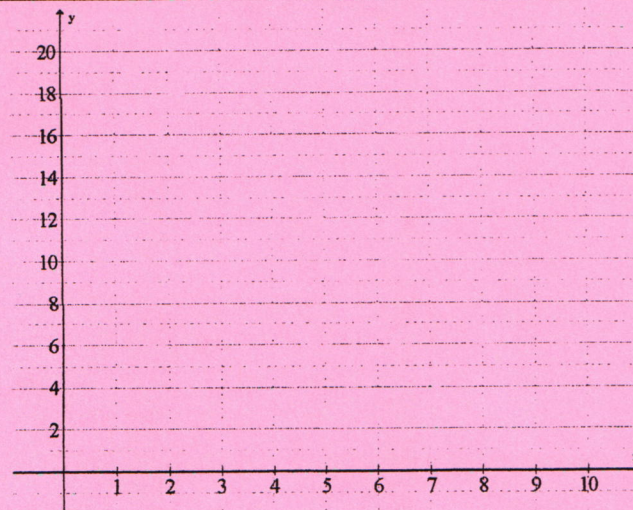
Constraints:

$$y \leq 12$$

$$y \leq -2x + 16$$

$$y \geq -0.5x + 3$$

$$y \geq 2x - 12$$



Vertices: (,) →

(,) →

(,) →

(,) →

(,) →

Which vertex gives the max value?Which vertex gives the min value?

Objective Function:

$$6x + 3y =$$

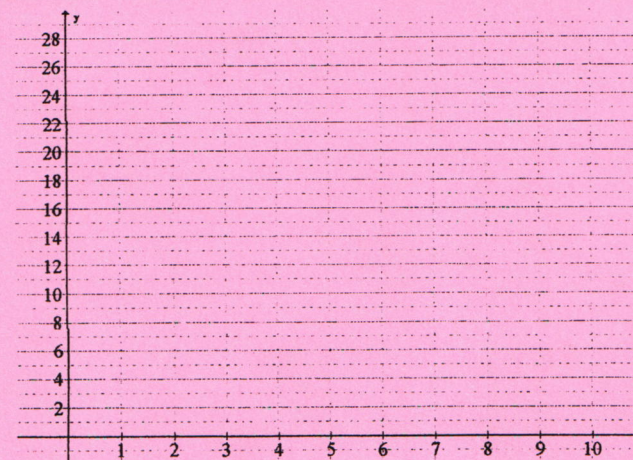
Constraints:

$$3x + y \leq 27$$

$$2x - y \geq -7$$

$$y \leq 9$$

$$y \geq -x + 7$$



Vertices: (,) →

(,) →

(,) →

(,) →

(,) →

Which vertex gives the max value?Which vertex gives the min value?