

# Station 1

Multiply the following Matrices.  
you do not need to show work.

1. 
$$\begin{bmatrix} 3 & 1 & -2 \\ 2 & -9 & 1 \\ 7 & 0 & 3 \end{bmatrix} \times \begin{bmatrix} -5 & 1 & -1 \\ 0 & 2 & -1 \\ 3 & 1 & 2 \end{bmatrix}$$

2. 
$$\begin{bmatrix} 3 & 1 \\ 6 & 2 \\ 0 & 1 \\ 1 & 9 \\ 2 & 4 \end{bmatrix} \times \begin{bmatrix} 6 \\ 7 \\ 0 \\ 1 \\ 2 \end{bmatrix}$$

3. 
$$\begin{bmatrix} 1 & 0 \\ -2 & -1 \\ 3 & 4 \\ 0 & -6 \end{bmatrix} \times \begin{bmatrix} -3 & 0 & 2 & 1 \\ 8 & 1 & -2 & 0 \end{bmatrix}$$

4. 
$$\begin{bmatrix} -3 & 0 & 2 & 1 \\ 8 & 1 & -2 & 0 \end{bmatrix} \times \begin{bmatrix} 1 & 0 \\ -2 & -1 \\ 3 & 4 \\ 0 & -6 \end{bmatrix}$$

## Station 2

5. Solve for  $x$  and  $y$ :

$$4 \begin{bmatrix} 3 & x \\ 7 & 2 \end{bmatrix} + \begin{bmatrix} 7 & 9 \\ y & 0 \end{bmatrix} = \begin{bmatrix} 19 & 25 \\ 20 & 8 \end{bmatrix}$$

6. Find the inverse of the matrix

$$\begin{bmatrix} 4 & 8 \\ 7 & 3 \end{bmatrix}$$

7. What happens when you multiply a matrix by its inverse?

8. What do you get when you multiply a matrix by an identity matrix?

9. a) Solve this system

$$3x + 2y = 28$$

$$6x - 5y = 38$$

b) What method did you use?

### Station 3

find the determinant for each of the following:

$$10. \begin{bmatrix} 2 & -3 \\ 7 & 6 \end{bmatrix}$$

$$11. \begin{bmatrix} 5 & 2 \\ 0 & 1 \end{bmatrix}$$

$$12. \begin{bmatrix} 4 & 2 & 3 \\ 5 & 1 & -1 \\ -2 & 0 & 6 \end{bmatrix}$$

$$13. \begin{bmatrix} 2 & 0 & -1 \\ 1 & 1 & -3 \\ 5 & -2 & 6 \end{bmatrix}$$

## Station 4

Use Cramer's rule to solve this system.

14.

$$x - y - z = -2$$

$$2x + 3y + z = 10$$

$$x - y - 4z = 4$$

- a) Determinant of the coefficient matrix
- b) Determinant of the  $x$  matrix
- c) Determinant of the  $y$  matrix
- d) Determinant of the  $z$  matrix

e  $x =$

$y =$

$z =$

Station 5  
~~xxxxxxxxxxxx~~

Find the area of a triangle

15. with vertices at  $(2, 7)$ ,  $(1, -2)$  and  $(-2, 3)$

Find the area of a triangle

16

With vertices at  $(3, 7)$ ,  $(3, -5)$  and  $(-2, -5)$

## Station 6

Solve for  $x$ ,  $y$  and  $z$ . (use any method)

$$17. \begin{bmatrix} 2 & 3 \\ 5x & 7 \end{bmatrix} + \begin{bmatrix} y & 9 \\ x & 12 \end{bmatrix} = \begin{bmatrix} -11 & 12 \\ 18 & z \end{bmatrix}$$

$$18. \begin{bmatrix} 1 & 0 \\ 3 & 6 \end{bmatrix} + y \begin{bmatrix} 2 & 1 \\ x & 5 \end{bmatrix} = \begin{bmatrix} 9 & z \\ 15 & 26 \end{bmatrix}$$

$$19. \begin{aligned} 2x + 5y &= 4 \end{aligned}$$

$$-x + 3y = -13$$

$$\begin{bmatrix} -21 & 3 & -8 \\ -7 & -15 & 9 \\ -26 & 10 & -1 \end{bmatrix}$$

2. Undefined

$$3. \begin{bmatrix} -3 & 0 & 2 & 1 \\ -2 & -1 & -2 & -2 \\ 23 & 4 & -2 & 3 \\ -48 & -6 & 12 & 0 \end{bmatrix}$$

$$4. \begin{bmatrix} 3 & 2 \\ 0 & -9 \end{bmatrix}$$

$$5. \quad 4x + 9 = 25$$

$$x = 4$$

$$4 \cdot 7 + y = 2$$

$$y = -8$$

$$6. \quad \begin{bmatrix} -\frac{3}{44} & \frac{2}{11} \\ \frac{7}{44} & -\frac{1}{11} \end{bmatrix}$$

7 you get an identity matrix

8 you get the same matrix

$$9. \quad x = 8$$

$$y = 2$$

reduced  
row  
echelon  
form

inverse matrices, Cramer's rule



⑩  $6 \cdot 2 - 7 \cdot (-3) = 12 - (-21) = 33$

⑪  $5 \cdot 1 - (0 \cdot 2) = 5 - 0 = 5$

⑫  $\begin{bmatrix} 4 & 2 & 3 \\ 5 & 1 & -1 \\ -2 & 0 & 6 \end{bmatrix} \begin{bmatrix} 4 & 2 \\ 5 & 1 \\ -2 & 0 \end{bmatrix} \rightarrow 24 + 10 + (-6) - (-6 + 0 + 60)$

~~33~~ ~~54~~ ~~14~~  
~~4~~

$28 - 54 = -26$

⑬  $\begin{bmatrix} 2 & 0 & -1 \\ 1 & 1 & -3 \\ 5 & -2 & 6 \end{bmatrix} \begin{bmatrix} 2 & 0 \\ 1 & 1 \\ 5 & -2 \end{bmatrix} \rightarrow 12 + 0 + 2 - (-5 + 12 + 0)$

$14 - 7$

$7$

14.  $\det [\text{coefficient matrix}] =$

$$\det [x \text{ matrix}] =$$

$$\det [y \text{-matrix}] =$$

$$\det [z \text{-matrix}] =$$

$$x = 0$$

$$y = 4$$

$$z = -2$$

15

$$\pm \frac{1}{2} \begin{vmatrix} 2 & 7 & 1 \\ 1 & -2 & 1 \\ -2 & 3 & 1 \end{vmatrix} = \pm \frac{1}{2} (-32) = 16$$

16

$$\pm \frac{1}{2} \begin{vmatrix} 3 & 7 & 1 \\ 3 & -5 & 1 \\ -2 & -5 & 1 \end{vmatrix} = \pm \frac{1}{2} (-60) = 30$$

$$\textcircled{12} \quad 2 + y = -11$$

$$y = -13$$

$$5x + x = 18$$

$$6x = 18$$

$$x = 3$$

$$7 + 12 = z$$

$$19 = z$$

$$\textcircled{18} \quad 1 + y \cdot 2 = 9$$

$$2y = 8$$

$$y = 4$$

$$3 + y \cdot x = 15$$

$$3 + 4x = 15$$

$$4x = 12$$

$$x = 3$$

$$0 + y \cdot 1 = z$$

$$0 + 4 \cdot 1 = z$$

$$4 = z$$

$$\textcircled{1} \quad \boxed{x = 3y + 3} \rightarrow 2(3y + 3) + 5y = 4$$

$$6y + 26 + 5y = 4$$

$$11y + 26 = 4$$

$$11y = -22$$

$$y = -2$$

$$\downarrow$$

$$2x + 5y = 4$$

$$2x - 10 = 4$$

$$2x = 14$$

$$x = 7$$